## DR. VIRENDRA SWARUP PUBLIC SCHOOL, KALYANPUR

## **Revision Worksheet**

Charter Polymerick

- Chapter: Polynomials
- 1. Factorize the following:  $9x^2 + 6x + 1 25y^2$ .
- 2. Factorize the following:  $a^2 + b^2 + 2ab + 2bc + 2ca$
- 3. Show that  $p(x) = x^3 3x^2 + 2x 6$  has only one real zero.
- **4.** Find the value of a if x + 6 is a factor of  $x^3 + 3x^2 + 4x + a$ .
- 5. If polynomials  $ax^3 + 3x^2 3$  and  $2x^3 5x + a$  leaves the same remainder when each is divided by x 4, find the value of a..
- 6. The polynomial  $f(x) = x^4 2x^3 + 3x^2 ax + b$  when divided by (x 1) and (x + 1) leaves the remainders 5 and 19 respectively. Find the values of a and b. Hence, find the remainder when f(x) is divided by (x 2).
- 7. If the polynomials  $2x^3 + ax^2 + 3x 5$  and  $x^3 + x^2 2x + a$  leave the same remainder when divided by (x 2), find the value of a. Also, find the remainder in each case.
- 8. If the polynomials  $az^3 + 4z^2 + 3z 4$  and  $z^3 4z + a$  leave the same remainder when divided by z 3, find the value of a.
- 9. The polynomial  $p(x) = x^4 2x^3 + 3x^2 ax + 3a 7$  when divided by x + 1 leaves the remainder 19. Find the values of a. Also find the remainder when p(x) is divided by x + 2.
- 10. Without actual division, prove that  $2x^4 5x^3 + 2x^2 x + 2$  is divisible by  $x^2 3x + 2$ .
- **12.** Simplify  $(2x 5y)^3 (2x + 5y)^3$ .
- **13.** Multiply  $x^2 + 4y^2 + z^2 + 2xy + xz 2yz$  by (-z + x 2y).
- **14.** If a + b + c = 5 and ab + bc + ca = 10, then prove that  $a^3 + b^3 + c^3 3abc = -25$ .
- **15.** Without actual division, prove that  $2x^4 6x^3 + 3x^2 + 3x 2$  is exactly divisible by  $x^2 3x + 2$ .
- **16.** Without actual division, prove that  $x^3 3x^2 13x + 15$  is exactly divisible by  $x^2 + 2x 3$ .
- 17. Find the values of a and b so that the polynomial  $x^3 10x^2 + ax + b$  is exactly divisible by (x 1) as well as (x 2).
- **18.** Find the integral zeroes of the polynomial  $2x^3 + 5x^2 5x 2$ .
- 19. Find the values of a and b so that the polynomial  $x^4 + ax^3 7x^2 + 8x + b$  is exactly divisible by (x + 2) as well as (x + 3).
- 20. If  $x^3 + ax^2 + bx + 6$  has (x 2) as a factor and leaves a remainder 3 when divided by (x 3), find the values of a and b
- **21.** Find the value of  $x^3 + y^3 + 15xy 125$  if x + y = 5.
- **22.** Without actually calculating, find the value of  $(25)^3 (75)^3 + (50)^3$ .
- **23.** Factorize each of the following cubic expressions:

(i) 
$$8x^3 - y - 12x^2y + 6xy^2$$

(ii) 
$$27q^3 - 125p^3 - 135q^2p + 225qp^2$$

**24.** Factorize:

(i) 
$$x^3 + 216y^3 + 8z^3 - 36xyz$$

(ii) 
$$a^3 - 64b^3 - 27c^3 - 36abc$$

$$(iii)\ 8x^3 + 729 + 108x^2 + 486x$$

- **25.** Give one example each of a binomial of degree 35, and of a monomial of degree 100.
- **26.** Find a zero of the polynomial p(x) = 2x + 1.
- **27.** Verify whether 2 and 0 are zeroes of the polynomial  $x^2 2x$ .
- 28. Find the zero of the polynomials in each of the following cases:

(i) 
$$p(x) = x + 5$$

(ii) 
$$p(x) = x - 5$$

(iii) 
$$p(x) = 2x + 5$$

(iv) 
$$p(x) = 3x - 2$$

$$(v) p(x) = 3x$$

(vi) 
$$p(x) = ax, a \neq 0$$

- **29.** Divide p(x) by g(x), where  $p(x) = x + 3x^2 1$  and g(x) = 1 + x.
- **30.** Divide the polynomial  $3x^4 4x^3 3x 1$  by x 1.
- **31.** Find the remainder obtained on dividing  $p(x) = x^3 + 1$  by x + 1.
- **32.** Find the remainder when  $x^4 + x^3 2x^2 + x + 1$  is divided by x 1.
- **33.** Check whether the polynomial  $q(t) = 4t^3 + 4t^2 t 1$  is a multiple of 2t + 1.
- **34.** Check whether p(x) is a multiple of g(x) or not, where  $p(x) = x^3 x + 1$ , g(x) = 2 3x.
- **35.** Find the remainder when  $x^3 ax^2 + 6x a$  is divided by x a.
- **36.** Examine whether x + 2 is a factor of  $x^3 + 3x^2 + 5x + 6$  and of 2x + 4.
- **37.** Find the value of k, if x 1 is a factor of  $4x^3 + 3x^2 4x + k$ .
- **38.** Find the value of a, if x a is a factor of  $x^3 ax^2 + 2x + a 1$ .
- **39.** Factorize  $6x^2 + 17x + 5$
- **40.** Factorize  $y^2 5y + 6$
- **41.** Factorize  $x^3 23x^2 + 142x 120$ .
- **42.** Factorize:

(i) 
$$x^3 - 2x^2 - x + 2$$
 (ii)  $x^3 - 3x^2 - 9x - 5$   
(iii)  $x^3 + 13x^2 + 32x + 20$  (iv)  $2y^3 + y^2 - 2y - 1$ 

- **43.** Factorize:  $4x^2 + 9y^2 + 16z^2 + 12xy 24yz 16xz$
- **44.** Expand  $(4a 2b 3c)^2$ .
- **45.** Factorize  $4x^2 + y^2 + z^2 4xy 2yz + 4xz$ .
- **46.** If x + 1 is a factor of ax3 + x2 2x + 4a 9, find the value of a.

